

2 курс (геометрические приложения кратных интегралов)

Найти объем тела, заданного ограничивающими его поверхностями.

1. $y = 16\sqrt{2x}$, $y = \sqrt{2x}$, $z = 0$, $x + z = 2$.
2. $y = 5\sqrt{x}$, $y = \frac{5x}{3}$, $z = 0$, $z = 5 + \frac{5\sqrt{x}}{3}$.
3. $x^2 + y^2 = 2$, $y = \sqrt{x}$, $y = 0$, $z = 0$, $z = 15x$.
4. $x + y = 2$, $y = \sqrt{x}$, $z = 12y$, $z = 0$.
5. $x = 20\sqrt{2y}$, $x = 5\sqrt{2y}$, $z = 0$, $z + y = \frac{1}{2}$.
6. $x = \frac{5\sqrt{y}}{2}$, $x = \frac{5y}{6}$, $z = 0$, $z = \frac{5}{6}(3 + \sqrt{y})$.
7. $x^2 + y^2 = 2$, $x = \sqrt{y}$, $x = 0$, $z = 0$, $z = 30y$.
8. $x + y = 2$, $x = \sqrt{y}$, $z = \frac{12x}{5}$, $z = 0$.
9. $y = 17\sqrt{2x}$, $y = 2\sqrt{2x}$, $z = 0$, $x + z = \frac{1}{2}$.
10. $y = \frac{5\sqrt{x}}{3}$, $y = \frac{5x}{9}$, $z = 0$, $z = \frac{5(3+\sqrt{x})}{9}$.
11. $x^2 + y^2 = 8$, $y = \sqrt{2x}$, $y = 0$, $z = 0$, $z = \frac{15x}{11}$.
12. $x + y = 4$, $y = \sqrt{2x}$, $z = 3y$, $z = 0$.
13. $x = \frac{5}{6}\sqrt{y}$, $x = \frac{5}{18}y$, $z = 0$, $z = \frac{5}{18}(3 + \sqrt{y})$.
14. $x = 19\sqrt{2y}$, $x = 4\sqrt{2y}$, $z = 0$, $z + y = 2$.
15. $x^2 + y^2 = 8$, $x = \sqrt{2y}$, $x = 0$, $z = \frac{30y}{11}$, $z = 0$.
16. $x + y = 4$, $x = \sqrt{2y}$, $z = \frac{3x}{5}$, $z = 0$.
17. $y = 6\sqrt{3x}$, $y = \sqrt{3x}$, $z = 0$, $x + z = 3$.
18. $y = \frac{5}{6}\sqrt{x}$, $y = \frac{5}{18}x$, $z = 0$, $z = \frac{5}{18}(3 + \sqrt{x})$.
19. $x^2 + y^2 = 18$, $y = \sqrt{3x}$, $y = 0$, $z = 0$, $z = \frac{5x}{11}$.
20. $x + y = 6$, $y = \sqrt{3x}$, $z = 4y$, $z = 0$.
21. $x = 7\sqrt{3y}$, $x = 2\sqrt{3y}$, $z = 0$, $z + y = 3$.
22. $x = \frac{5\sqrt{y}}{3}$, $x = \frac{5y}{9}$, $z = 0$, $z = \frac{5(3+\sqrt{y})}{9}$.

23. $x^2 + y^2 = 18$, $x = \sqrt{3y}$, $x = 0$, $z = 0$, $z = \frac{10y}{11}$.

24. $x + y = 6$, $x = \sqrt{3y}$, $z = \frac{4x}{5}$, $z = 0$.

25. $y = \sqrt{15x}$, $y = \sqrt{15x}$, $z = 0$, $z = \frac{10y}{11}$.